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*Evolutionary Equations with Material Laws Containing Fractional Integrals*

### Abstract

A well-posedness strategy for a time-shift invariant class of evolutionary operator equations as discussed in [1, 2] is applied to material laws involving fractional time-integration. This leads to evolutionary problems with fractional time-derivatives. Fractional time-differentiation is established in the framework of an function calculus for the time derivative  $\partial_0$  as a normal operator. A class of such material laws of the form

$$\sum_{\alpha \in \Pi} \partial_0^{-\alpha} M_\alpha$$

with bounded, linear coefficient operator  $M_\alpha : H \rightarrow H$ ,  $\alpha \in \Pi$ ,  $H$  Hilbert space, where  $\Pi$  is a finite subset of  $[0, 1]$ , is characterized, for which well-posedness of the corresponding evolutionary problem

$$\left( \sum_{\alpha \in \Pi} \partial_0^{1-\alpha} M_\alpha + A \right) U = f,$$

where for example  $A$  is skew-selfadjoint in  $H$ , can be shown. The approach is exemplified by an application to a fractional Kelvin-Voigt type model in solid mechanics.

### BIBLIOGRAPHY

- [1] Picard, R. and McGhee, D. F., *Partial Differential Equations: A Unified Hilbert Space Approach*, Volume 55 of *De Gruyter Expositions in Mathematics*. De Gruyter. Berlin, New York. 518 p., (2011).
- [2] Picard, R., *A Class of Evolutionary Problems with an Application to Acoustic Waves with Impedance Type Boundary Conditions*, volume 221 of *Operator Theory, Advances and Applications*, pages 533–548. Birkhäuser Science, Springer, Berlin, (2012).