

**(R1)-(R10)**

$$(R1) \quad a + b = b + a \quad (\text{和の交換律})$$

$$(R2) \quad (a + b) + c = a + (b + c) \quad (\text{和の結合律})$$

$$(R3) \quad \exists 0 \in \mathbb{R}, \\ \forall a \in \mathbb{R}, \quad a + 0 = 0 + a = a \quad (\text{零元の存在})$$

$$(R4) \quad \forall a \in \mathbb{R}, \quad \exists -a \in \mathbb{R}, \\ a + (-a) = (-a) + a = 0 \quad (\text{和の逆元の存在})$$

$$(R5) \quad a \cdot b = b \cdot a \quad (\text{積の交換律})$$

$$(R6) \quad (a \cdot b) \cdot c = a \cdot (b \cdot c) \quad (\text{積の結合律})$$

$$(R7) \quad \exists 1 \in \mathbb{R}, \quad \forall a \in \mathbb{R}, \\ 1 \cdot a = a \cdot 1 = a \quad (\text{単位元の存在})$$

$$(R8) \quad \forall a \in \mathbb{R} \setminus \{0\}, \\ \exists a^{-1} \in \mathbb{R}, \quad a \cdot a^{-1} = a^{-1} \cdot a = 1 \quad (\text{積の逆元の存在})$$

$$(R9) \quad a \cdot (b + c) = a \cdot b + a \cdot c, \\ (a + b) \cdot c = a \cdot c + b \cdot c \quad (\text{分配律})$$

$$(R10) \quad 1 \neq 0 \quad (0 \text{ 以外の元の存在})$$